

Statistical properties of the repeating fast radio burst source FRB 121102

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Abstract

Currently, FRB 121102 is the only fast radio burst source that was observed to give out bursts repeatedly. It shows a high repeating rate, with more than one hundred bursts being spotted, but with no obvious periodicity in the activities. Thanks to its repetition, the source was well localized with a subarcsecond accuracy, leading to a red shift measurement of about 0.2. FRB 121102 is a unique source that can help us understand the enigmatic nature of fast radio bursts. In this study, we analyze the characteristics of the waiting times between bursts from FRB 121102. It is found that there is a clear bimodal distribution for the waiting times. While most waiting times cluster at several hundred seconds, a small portion of the waiting times are strikingly in the range of 2-40 millisecond. More interestingly, it is found that the waiting time does not correlate with the burst intensity, either for the preceding burst or for the subsequent burst. It strongly indicates that the repeating bursts should be generated by some external mechanisms, but not internal mechanisms. As a result, the models involving collisions between small bodies and neutron stars could be competitive mechanisms for this interesting source.

Keywords: Fast radio bursts (FRBs); FRB 121102; Galactic pulsars; Neutron Stars; Black Holes

Introduction

Fast radio bursts (FRBs) are intense extragalactic radio bursts with a flux of Jy level and with short durations of about several millisecond. Their origin and trigger mechanism is still an open question. The first FRB event (010724) was once named according to the discoverer as "Lorimer Burst" [1]. After about one decade, more than 60 FRBs have been found by terrestrial radio telescopes [2]¹. FRBs have anomalously high dispersion measures (DMs), significantly exceeding the expected Milky Way contribution along the line of sight, which is contrary to Galactic pulsars [3-10] (but note that low DM has also been hinted from two FRBs [11, 12] and a candidate (FRB 141113) [13]). It indicates that FRBs are of extragalactic or even cosmological origin, rather than of Galactic origin [14-18]. Their bright millisecond radio pulses with a high scattering effect point to extremely high brightness temperatures, which implies that luminous coherent emission processes around compact objects should be involved, which might include the curvature radiation (also known as the "antenna" mechanism) [19-21], or the synchrotron maser emission [22-25]. However, the exact mechanism is still enigmatic and greatly debated [26-27].

Numerous theoretical models have been proposed to account for such an enigmatic class of radio transients. The number of models is almost comparable to that of the observed FRBs up to date [28, 29]. Most of those progenitor models involve compact objects (e.g., Neutron Stars (NS), Black Holes (BH) and White Dwarfs (WD)) outside of the Milky Way. Popular mechanisms include: mergers of binary NS [30-32], or binary WD [33], or NS-WD binary [34, 35], or NS/WD-BH binary [36-38], the interactions of pulsar-BH systems [39] or Kerr-Newman BH-BH [40, 41], collapse of compact objects (e.g., collapse of NS [42-46], collapse of strange star crust [47], giant pulses/flares from magnetars or young pulsars [48-51], and other supernovae interrelated theories [22, 52-55]. A few other models include: mechanisms related to active galactic nuclei (AGN) and Kerr-BH or Strange Star interactions [56-60], collisions between NSs and small bodies [61-64], Axion star collides with a NS/BH [65-67], interactions between Axions and compact bodies [68-70], explosions such as star quakes [71], primordial BHs/Planck stars collapse to form white holes [72, 73], lightning/wandering in pulsars [16, 74], or NS combing [75, 76], and so on. In short, while the true mechanisms of FRBs are still unclear, it is possible that multiple populations of FRBs might exist [77-79]. For a summary of FRB progenitor models, see the recent article of Platts et al. [80] and the online version of a tabulated summary².

¹Petroff et al. 2016 catalogued and updated all published sample of FRBs, see their online catalog-<http://www.frbcat.org>

²<http://frbtheorycat.org>

In general, the above models could be grouped into two different categories [81, 82], i.e. catastrophic models and non-catastrophic models. Following this idea, a key issue is then whether the observed FRBs are repetitive or not. Strangely enough, among the more than 60 FRB sources, only one event, i.e. FRB 121102 is observed to repeatedly burst out, which actually has produced hundreds of bursts so far. For all the other FRB sources, no indication of repetition was observed although long-term monitoring had been extensively carried out [1, 3, 9, 11, 83-86]. However, strictly speaking, it still remains obscure how many FRBs are repetitive and whether their repetition is similar to the unique FRB 121102 or not. In this study, we will mainly concentrate on the repeating event of FRB 121102.

FRB 121102 was initially discovered through the 305-m Arecibo telescope Pulsar Survey Project (ALFA) [87]. It is the first and the only known burst that has been successfully identified to be associated with a host galaxy, a small low-metallicity star-forming dwarf galaxy at $z = 0.19273 \pm 0.00008$ [89-92]. It is also the only burst with a repeating behavior [92]. Hundreds of additional bursts have been observed from the same direction toward FRB 121102 (the position is known to sub-arc second precision) and the measured DMs of all these bursts (between 553 – 569 pc cm^{-3}) are consistent with the first burst of 121102. These consequent observations were made discontinuously by many terrestrial radio telescopes such as the Arecibo telescope (AO), the Green Bank Hydrogen

telescope (GBT), the Karl G. Jansky Very Large Array (VLA), the 100-m Effelsberg telescope (Eff), and the Apertif Radio Transient System (ARTS), at multiple radio bands [77, 88, 92-101]. They all reveal no additional waveband sporadic emission [88, 93, 102-103], and there is no evidence for any periodicity [100]. It is interesting that a cosmological origin is confirmed for FRB 121102 confirms with the red shift measurement. The catastrophic models are also ruled out for this source. FRB 121102 is associated with a variable radio source with a continuum non-thermal spectrum. It seems to be a low-luminosity AGN or other kind of unknown peculiar source [88]. An AGN scenario thus remains possible [56-59], but it could also be due to other mechanisms such as a young neutron star with pulsar wind nebula [48-51], or a neutron star interacting with small bodies [62-64].

For a sporadically repeating astrophysical phenomenon, the temporal information or quantities (e.g., duration, elapsed time, periodicity, episodic time) of outbursts play an important role in understanding the central engine, and revealing the radiation mechanism and energy dissipation processes. For instance, the previous researches on the non-stationary Poisson process of soft gamma-ray repeaters [104-106], pulsar glitches [107-109], anomalous X-ray pulsars (AXPs) [110, 111], X-ray flares in γ ray burst afterglows [112, 113], can give us helpful references. A time-variable system always shows some kind of irregularity. Especially the time interval between two adjacent bursts, which is known as the waiting time (here after WT or Δt), is an important parameter that could provide valuable information on the central engine.

Previously, Gu et al. (2016) established a relation between the waiting time and the mass transfer rate of accretion in a NS-WD binary merger [34], which can be somewhat related to the observed behaviors of FRB 121102. Katz (2018) found the distribution of the waiting times between bursts of FRB 121102 are apparently far from a Poissonian form, and proposed that such a distribution may be consistent with a precessing jet launched from a NS or a BH accretion disc [114]. Wang et al. (2018) found that the energy and waiting time distributions of FRB 121102 derived from the paper [99] show an earthquake-like behavior. They argued that those bursts could be powered by some star quake-like mechanisms [71]. Palaniswamy et al. (2018) compared 40 bursts of FRB 121102 with other non-repeating FRBs on the observed waiting time-flux ratio plane. They found that their distribution is well separated from other FRBs in the plane, suggesting that there could be multiple populations of FRBs [78]. In this study, with more observed bursts (on the level of hundred) from the repeating source FRB 121102, we re-analyze the waiting time statistics. Especially, we study the correlation between the waiting time and the flux and other parameters of the repeating bursts. It is expected that these new studies will help us understand the nature of this unique source.

The structure of our paper is organized as follows. In Section II, we collect the detailed observational data for the repeated bursts from FRB 121102. We then calculate the waiting times for the available events. In Section III, we derive

the waiting time distribution and analysis its correlation with other parameters. The implication of our study for the nature of the repeater is presented. Finally, Section IV presents our conclusions and some further discussion.

The Observations and Samples of FRB 121102

FRB 121102 is currently the only source to exhibit repeating bursts among the FRB population. From the literature, we have collected all the observational data of the observed bursts from this source. An overview of the available observations is listed in (Table 1). In this table, we present the date of observations, the telescope names, the starting time of the observation, the duration of the corresponding monitoring, number of bursts observed during the observational campaign, the number of available waiting times during the period, and references. Note that in each observational campaign, the source usually could be monitored continuously for several thousands (or up to several hours in several cases). A meaningful waiting time could be derived only for two bursts that are observed in the same observational campaign. For example, if 5 bursts were observed in a continuous observational campaign, then 4 waiting time could be derived from these 5 bursts.

Up to now, there are thirty-five continuous observation campaigns on FRB 121102 that resulted in successful detection of at least one fast radio burst from the source. A lot of bursts are detected in Observation Campaigns 33 and 34, i.e. 46 and 47 bursts were observed, respectively. In summary, more than one burst was detected in 17 observations (see the sixth column in Table 1), providing us with 171 bursts in total, as listed in table 2 at the end of this article.

Table 1. Log of the observations on FRB 121102

Obs. number	Date yyyy/mm/dd	Telescope /Receiver	Start Time hh/mm/ss	Obs. Length t _{obs}	Number of Bursts	Waiting time number	Reference
1	2012/11/02	AO/ALFA	06:38:13	~200	1	0	[88, 93, 94]
2	2015/05/17	AO/ALFA	17:45:38	1002	2	1	[93]
3	2015/06/02	AO/ALFA	16:38:47	1002	2	1	[93]
4	2015/06/02	AO/ALFA	17:48:52	1002	6	5	[93]
5	2015/11/13	GBT/S-band	07:42:09	3000	1	0	[94]
6	2015/11/19	GBT/S-band	10:14:57	3000	4	3	[94]
7	2015/12/08	AO/L-wide	04:43:24	3625	1	0	[94]
8	2016/08/20	Eff/5 GHz	09:23:40	1200	3	2	[101]
9	2016/08/23	VLA/3 GHz	17:26:28	3240	1	0	[89, 96]
10	2016/09/02	VLA/3 GHz	15:52:17	3240	2	1	[89, 96]
11	2016/09/07	VLA/3 GHz	10:14:50	7200	1	0	[89, 96]
12	2016/09/12	VLA/3 GHz	09:15:19	7200	1	0	[89, 96]
13 ^a	2016/09/14	VLA/3 GHz	09:20:23	7200	1	0	[89, 96]
14	2016/09/15	VLA/3 GHz	09:16:29	7200	1	0	[89, 96]
15	2016/09/16	GBT/S-band	03:59:12	14452	2	1	[98]
16 ^b	2016/09/17	VLA/3 GHz	08:59:20	7200	1	0	[89, 96]
17	2016/09/18	GBT/S-band	04:02:15	14269	2	1	[98]
18 ^a	2016/09/18	VLA/3 GHz	08:59:27	7200	1	0	[89, 96]
19	2016/12/25	AO4.1-4.9 GHz	02:48:51.998	6703	10	9	[78]

20	2016/12/26	AO4.1-4.9 GHz	02:44:21.998	6806	5	4	[78]
21 ^c	2017/01/11	GBT/S-band	23:13:56	19869	6	5	[98]
22 ^c	2017/01/12	AO/L-wide	01:46:27	6270	4	3	[98]
23	2017/01/16	Eff/L-band	16:14:20	14400	3	2	[95]
24	2017/01/19	AO4.1-4.9GHz	01:25:03	5901	1	0	[78]
25	2017/01/19	Eff/L-band	16:05:40	12630	5	4	[95]
26	2017/01/25	Eff/L-band	16:22:00	12600	4	3	[95]
27	2017/02/15	AO/WE.G-1.38 GHz			1	0	[99]
28	2017/02/19	Eff/L-band	14:28:40	10800	1	0	[95]
19	2017/02/22	AO/WE.G-1.38 GHz			1	0	[99]
30	2017/02/22	AO/WE.G-1.38 GHz			1	0	[99]
31	2017/02/24	AO/WE.G-1.38 GHz			1	0	[99]
32	2017/03/02	AO/WE.G-1.38 GHz			1	0	[99]
33	2017/08/26	GBT/C-band	13:51:44	1800	46 ^d	45	[100, 102]
34	2017/08/26	GBT/C-band	14:21:59	1800	47 ^d	46	[100, 102]
35	2017/08/31	ARTS/L-wide	06:23:37	3600	1	0	[97]

Note: Each observation campaign is marked with a sequence number according to the start time, as shown in Column 1. Column 2 is the observation date; Column 3 presents the receiver and telescope name; Column 4 gives the start time of the observation; Column 5 gives observation duration; Column 6 gives the number of FRBs observed during the campaign, and Column 7 is the number of available waiting times; Column 8 provides the references.

^aIn these observations, the source was monitored at AO/L-wide but the observations gave non-detection results.

^bIn these observations, one burst was detected both by the VLA fast-dump observations at 3 GHz band and Arecibo observations with L-wide receiver at a frequency range of 1.15 – 1.73 GHz.

^cIn these observations, the observation time was crossing, and two bursts were detected both by GBT/S-band and AO/L-band receiver [97].

^dObservations by the GBT/4 – 8 GHz (or C-band) receiver with Breakthrough Listen digital backend. Due to successful application of deep learning [101], the number of bursts is tremendous above 5.2 GHz. Note that in these two observations, 21 bursts have been published earlier by Gajjar et al. 2018 [99]. Here we only consider Zhang’s results [101].

We have calculated the waiting times for those successive bursts detected in a continuous observation. The waiting time (WT, Δt) is defined as the time interval between two neighboring and non-piled-up bursts in a continuous and uninterrupted observation campaign. For the repetitive fast radio bursts from FRB 121102, the observed profiles are composed of only a single pulse. In our calculations, we ignored the time dilation factor of 1+z, which is not large and will not affect our analysis. As a result, the number of waiting times available is 136, as listed in Column 4 of (Table 2). In table 2, we also listed some other important parameters such as the peak flux density, the fluence, the duration, etc.

Table 2. The waiting time and a few key parameters of the repeating bursts from FRB 121102.
For the references of the observational data, please see (Table 1).

Burst No.	BPT (MJD)	TOA (day)	WT (s)	Center frequency (MHz)	Bandwidth (MHz)	S (Jy)	σ_S	F (Jyms)	σ_F	w (ms)	σ_w
1	56233.282837008			1375	322	0.040	0.008	0.10	0.012	3.3	0.30
2	57159.737600835	926.4548	572.2085	1375	322	0.030	0.006	0.10	0.012	3.8	0.40
3	57159.744223619	926.4614		1375	322	0.030	0.006	0.10	0.012	3.3	0.40
4	57175.693143232	942.4103	568.9089	1375	322	0.040	0.008	0.20	0.012	4.6	0.30
5	57175.699727826	942.4169		1375	322	0.020	0.004	0.09	0.030	8.7	1.50
6	57175.742576706	942.4597	22.6919	1375	322	0.020	0.004	0.06	0.008	2.8	0.40
7	57175.742839344	942.4600	57.9782	1375	322	0.020	0.004	0.06	0.028	6.1	1.40
8	57175.743510388	942.4607	186.2304	1375	322	0.140	0.028	0.90	0.014	6.6	0.10
9	57175.745665832	942.4628	169.2592	1375	322	0.050	0.01	0.30	0.015	6.0	0.30
10	57175.747624851	942.4648	57.2326	1375	322	0.050	0.01	0.20	0.025	8.0	0.50
11	57175.748287265	942.4655		1375	322	0.310	0.062	1.00	0.012	3.06	0.04
12	57339.356046005567	1106.0732		2000	800	0.040		0.20	0.045	6.73	1.12
13	57345.447691250090	1112.1649	414.4327	2000	800	0.060		0.40	0.034	6.10	0.57
14	57345.452487925162	1112.1697	441.2775	2000	800	0.040		0.20	0.040	6.14	1.00
15	57345.457595303807	1112.1748	416.2582	2000	800	0.020		0.08	0.028	4.30	1.40
16	57345.462413106565	1112.1796		2000	800	0.090		0.60	0.032	5.97	0.35
17	57364.204632665605	1130.9218		1430	700	0.030	0.006	0.09	0.007	2.50	0.23
18	57620.392218422	1387.1094	160.3673	4850		0.3	0.04	0.15	0.05	0.5	0.10
19	57620.394074525	1387.1112	480.0102	4850		0.2	0.04	0.12	0.044	0.6	0.10
20	57620.399630199	1387.1168		4850		0.1	0.02	0.17	0.064	1.7	0.30
21	57623.74402686	1390.4612		3000	512	0.120		0.60		5.0	
22	57633.67986367	1400.3970	1321.5493	3000	500	0.670		3.35		5.0	
23	57633.69515938	1400.4123		3000	500	0.025		0.13		5.0	
24	57638.49937435	1405.2165		3000	500	0.063		0.32		5.0	
25	57643.45730263	1410.1745		3000	500	0.326		1.63		5.0	
26	57645.42958602	1412.1467		3000	500	0.039		0.20		5.0	
27	57646.46600650	1413.1832		3000	500	0.050		0.25		5.0	
28	57647.232346450619	1413.9495	0.0374	2000	800	0.360		0.32	0.022	2.16	0.06
29	57647.232346883015	1413.9495		2000	800	0.080		0.16	0.020	1.94	0.25
30	57648.43691490	1415.1541		3000	500	0.086	0.014	0.43		5.0	
31	57649.173812898174	1415.8910	3836.1884	2000	800	0.360		1.32	0.025	3.45	0.07
32	57649.218213226581	1415.9354		2000	800	0.290		0.34	0.020	0.88	0.07
33	57649.45175697	1416.1689		3000	500	0.159	0.006	0.80		5.0	
34	57747.1295649013	1513.8467	658.5214	4500	800	0.9	0.18	0.7	0.14	0.8	0.01
35	57747.1371866766	1513.8543	784.8879	4500	800	0.3	0.06	0.2	0.04	0.85	0.01
36	57747.1462710273	1513.8634	458.1716	4500	800	0.8	0.16	0.2	0.04	0.22	0.01
37	57747.1515739398	1513.8687	250.0029	4500	800	0.2	0.04	0.09	0.018	0.55	0.01
38	57747.1544674918	1513.8716	503.0038	4500	800	0.2	0.04	0.1	0.02	0.76	0.01
39	57747.1602892954	1513.8775	4.7001	4500	800	1.8	0.36	0.05	0.01	0.03	0.01
40	57747.1603436945	1513.8775	473.8184	4500	800	0.6	0.12	0.2	0.04	0.31	0.01
41	57747.1658277033	1513.8830	47.2859	4500	800	0.4	0.08	0.5	0.1	1.36	0.01
42	57747.1663749941	1513.8835	828.7868	4500	800	0.2	0.04	0.3	0.06	1.92	0.01
43	57747.1759674338	1513.8931		4500	800	0.2	0.04	0.2	0.04	0.98	0.01
44	57748.1256436428	1514.8428	2408.9006	4500	800	0.1	0.02	0.1	0.02	0.95	0.01
45	57748.1535244366	1514.8707	146.0587	4500	800	0.4	0.08	0.2	0.04	0.42	0.01
46	57748.1552149312	1514.8724	206.7319	4500	800	0.8	0.16	0.6	0.12	0.78	0.01
47	57748.1576076618	1514.8748	1562.9040	4500	800	1.2	0.24	0.2	0.04	0.15	0.01
48	57748.1756968287	1514.8929		4500	800	0.4	0.08	0.4	0.08	0.54	0.01
49	57765.049526345771	1531.7667	1319.0573	2000	800	0.17		0.33	0.015	1.40	0.09
50	57765.064793212950	1531.7820	367.5706	2000	800	0.38		0.83	0.015	1.79	0.04
51	57765.069047502300	1531.7862	2745.8220	2000	800	0.20		0.62	0.024	2.97	0.12
52	57765.100827849608	1531.8180	0.0008	1380	800	0.09	0.018	0.37	0.010	4.29	0.11
53	57765.100827859293	1531.8180	678.4977	2000	800	0.09		0.18	0.025	2.46	0.28
54	57765.108680842022	1531.8258	1045.2119	1380	800	0.02	0.004	0.03	0.002	3.69	0.11
55	57765.120778202479	1531.8379	0.0002	1380	800	0.02	0.004	0.05	0.009	4.34	0.44
56	57765.120778204779	1531.8379	1358.2429	2000	800	0.56		1.08	0.017	1.36	0.03
57	57765.136498608757	1531.8537	590.8832	2000	800	0.11		0.22	0.019	1.68	0.17
58	57765.143337535257	1531.8605		1380	800	0.03	0.006	0.10	0.010	3.66	0.32

59	57769.6881141561	1536.4053	1225.7660	1360	300	0.7	0.1	2.6	0.40	3.56	0.09
60	57769.702301263	1536.4195	5328.0127	1360	300	0.17	0.03	0.6	0.10	3.400	0.40
61	57769.7639680761	1536.4811		1360	300	0.8	0.1	1.7	0.30	2.050	0.06
62	57772.1290302972	1538.8462		4500	800	0.8	0.16	0.6	0.12	0.74	0.01
63	57772.6649755688	1539.3821	1990.5243	1360	300	0.36	0.05	0.7	0.10	2.100	0.10
64	57772.688014045	1539.4052	6089.6034	1360	300	0.11	0.02	0.35	0.09	3.200	0.70
65	57772.758495566	1539.4757	337.0257	1360	300	0.25	0.04	1.3	0.20	5.100	0.30
66	57772.762396326	1539.4796	1928.7907	1360	300	0.22	0.03	0.4	0.07	1.800	0.20
67	57772.784720292	1539.5019		1360	300	0.21	0.03	0.4	0.09	1.900	0.30
68	57778.6885027615	1545.4057	5855.1556	1360	300	0.39	0.06	1	0.20	2.600	0.10
69	57778.756270766	1545.4734	0.0341	1360	300	0.11	0.02	0.23	0.06	2.100	0.40
70	57778.756271161	1545.4734	3708.5134	1360	300	0.18	0.03	0.5	0.10	2.900	0.30
71	57778.799193770	1545.5164		1360	300	0.21	0.03	0.38	0.07	1.800	0.20
72	57799.983175660	1566.7003		1380	800	1.4	0.28	8.022	1.604	5.73	
73	57803.692917989	1570.4101		1360	300	0.21	0.03	0.7	0.10	3.500	0.30
74	57806.964250780	1573.6814	1769.3225	1380	800	1.6	0.32	3.936	0.787	2.46	
75	57806.984729050	1573.7019		1380	800	1.5	0.3	5.535	1.107	3.69	
76	57808.002785850	1574.7199		1380	800	0.79	0.158	2.915	0.583	3.69	
77	57814.946985200	1581.6641		1380	800	0.47	0.094	0.541	0.108	1.15	
78	57991.4099040442	1758.1276	2.2185	7020	3900	0.7635	0.0105	0.6061	0.0212	1.43	
79	57991.4099297208	1758.1271	7.9579	7050	2300	0.0348	0.0081	0.0256	0.0201	2.15	
80	57991.4100218264	1758.1272	4.1287	7020	2400	0.0539	0.0083	0.0505	0.0168	1.43	
81	57991.4100696130	1758.1272	128.6319	6170	2500	0.0541	0.0084	0.0906	0.0225	2.51	
82	57991.4115584078	1758.1287	45.5501	5560	2500	0.0457	0.0084	0.053	0.019	1.79	
83	57991.4120856083	1758.1292	19.5705	5470	1400	0.0318	0.0064	0.0435	0.0144	1.79	
84	57991.4123121182	1758.1295	39.1048	7020	2400	0.0449	0.0083	0.0264	0.0146	1.08	
85	57991.4127647200	1758.1299	0.0143	5550	3900	0.0972	0.0105	0.0664	0.0212	1.43	
86	57991.4127648858	1758.1299	13.9614	5450	2900	0.0569	0.0091	0.0673	0.0206	1.79	
87	57991.4129264759	1758.1301	8.0693	5440	2000	0.0719	0.0092	0.1461	0.0294	3.58	
88	57991.4130198711	1758.1302	29.6054	7030	1800	0.138	0.0072	0.0566	0.0103	0.72	
89	57991.4133625264	1758.1305	8.3149	7030	1800	0.0448	0.0072	0.0468	0.0146	1.43	
90	57991.4134587642	1758.1306	21.4177	7060	4000	0.4521	0.0106	0.3632	0.0186	1.08	
91	57991.4137066537	1758.1309	11.2669	7110	4000	0.3421	0.0106	0.2628	0.0185	1.08	
92	57991.4138370580	1758.1310	198.3099	7030	4000	0.3182	0.0106	0.2646	0.0215	1.43	
93	57991.4161323109	1758.1332	4.5723	7010	2900	0.0328	0.0091	0.0353	0.0207	1.79	
94	57991.4161852305	1758.1333	1.9554	7020	2400	0.0375	0.0083	0.0462	0.0188	1.79	
95	57991.4162078619	1758.1334	19.7797	5720	2000	0.0384	0.0075	0.0229	0.0132	1.08	
96	57991.4164367935	1758.1336	16.9835	5470	3900	0.0689	0.0106	0.0362	0.0185	1.08	
97	57991.4166333622	1758.1338	54.9513	7020	3900	0.5637	0.0105	0.3492	0.0184	1.08	
98	57991.4172693722	1758.1344	9.6220	5800	2500	0.0732	0.0084	0.0526	0.0148	1.08	
99	57991.4173807378	1758.1345	28.8562	6450	1900	0.0723	0.0074	0.0295	0.0106	0.72	
100	57991.4177147221	1758.1349	13.0318	5750	2500	0.0542	0.0084	0.0352	0.0147	1.08	
101	57991.4178655533	1758.1350	65.8063	6410	3900	0.136	0.0105	0.0811	0.0184	1.08	
102	57991.4186272003	1758.1358	34.6894	7610	3900	0.1288	0.0105	0.0978	0.0213	1.43	
103	57991.4190286984	1758.1362	36.3906	5750	2000	0.0541	0.0075	0.0401	0.0151	1.43	
104	57991.4194498856	1758.1366	0.0052	5750	1700	0.0508	0.0069	0.0446	0.0139	1.43	
105	57991.4194499461	1758.1366	0.0019	7110	1000	0.04	0.0054	0.0213	0.0095	1.08	
106	57991.4194499686	1758.1366	1.0948	6220	2600	0.0496	0.0068	0.0362	0.012	1.08	
107	57991.4194626399	1758.1366	0.0193	5720	2000	0.039	0.0075	0.0256	0.017	1.79	
108	57991.4194628627	1758.1366	121.3916	6230	1900	0.0293	0.0074	0.0295	0.015	1.43	
109	57991.4208678576	1758.1380	29.8121	7110	1300	0.0391	0.0061	0.0286	0.0123	1.43	
110	57991.4212129047	1758.1384	43.1795	7110	4000	0.1268	0.0106	0.0607	0.0151	0.72	
111	57991.4217126673	1758.1389	35.3103	5670	3900	0.1858	0.0106	0.0785	0.0151	0.72	
112	57991.4221213510	1758.1393	1.3489	5720	2000	0.064	0.0075	0.0682	0.017	1.79	
113	57991.4221369638	1758.1393	69.3354	6900	2400	0.0557	0.0082	0.0397	0.0187	1.79	
114	57991.4229394568	1758.1401	5.6751	6200	3900	0.2147	0.0105	0.1312	0.0238	1.79	
115	57991.4230051411	1758.1402	109.3405	5770	4000	0.0355	0.0106	0.0263	0.0263	2.15	
116	57991.4242706565	1758.1414	23.1794	6230	1900	0.0456	0.0074	0.053	0.0168	1.79	
117	57991.4245389366	1758.1417	119.2321	5250	900	0.0312	0.0051	0.0174	0.009	1.08	
118	57991.4259189384	1758.1431	41.0301	5750	900	0.0245	0.0051	0.0287	0.0127	2.15	
119	57991.4263938242	1758.1436	13.7109	6170	1900	0.0561	0.0074	0.0675	0.0183	2.15	
120	57991.4265525154	1758.1437	158.9548	6170	3900	0.3922	0.0105	0.1565	0.0151	0.72	

121	57991.4283922705	1758.1456	17.3030	7140	2400	0.0574	0.0082	0.0746	0.022	2.51	
122	57991.4285925362	1758.1458	158.5758	4780	3900	0.063	0.0105	0.0362	0.0184	1.08	
123	57991.4304279044	1758.1476	57.7644	5670	3900	0.0704	0.0106	0.051	0.0185	1.08	
124	57991.4310964736	1758.1483	49.7042	6160	1400	0.0271	0.0064	0.0574	0.0193	3.23	
125	57991.4316717532	1758.1488	26.1148	6080	2000	0.0424	0.0075	0.0412	0.0169	1.79	
126	57991.4319740079	1758.1491	26.0491	5660	3900	0.2084	0.0105	0.1629	0.0185	1.08	
127	57991.4322755018	1758.1494	221.1596	5520	2000	0.058	0.0075	0.048	0.0151	1.43	
128	57991.4348352197	1758.1520	31.3033	5730	1900	0.0288	0.0074	0.0243	0.0167	1.79	
129	57991.4351975268	1758.1524	117.4965	7090	1900	0.0614	0.0073	0.0561	0.0149	1.43	
130	57991.4365574396	1758.1537	111.6369	7120	1900	0.0715	0.0073	0.0564	0.0128	1.08	
131	57991.4378495339	1758.1550	55.2223	6910	2300	0.041	0.0082	0.0244	0.0144	1.08	
132	57991.4384886807	1758.1557	75.3406	5520	1500	0.042	0.0064	0.0224	0.0113	1.08	
133	57991.4393606779	1758.1565	591.9158	7110	4000	0.2362	0.0106	0.2342	0.0239	1.79	
134	57991.4462115554	1758.1634	67.1154	6160	1400	0.0387	0.0064	0.018	0.0091	0.72	
135	57991.4469883544	1758.1642	81.2813	6440	1500	0.0395	0.0065	0.0131	0.0093	0.72	
136	57991.4479291105	1758.1651	10.2570	5580	2900	0.0334	0.0091	0.0523	0.0244	2.51	
137	57991.4480478257	1758.1652	32.8169	4970	900	0.0179	0.0051	0.0258	0.0128	2.15	
138	57991.4484276509	1758.1656	151.8190	5580	3900	0.21	0.0105	0.1375	0.0184	1.08	
139	57991.4501848147	1758.1673	24.4345	5390	1400	0.0463	0.0063	0.0197	0.009	0.72	
140	57991.4504676214	1758.1676	222.2426	7470	2300	0.0405	0.0081	0.0343	0.0164	1.43	
141	57991.4530398739	1758.1702	472.8758	4780	2400	0.0843	0.0083	0.0672	0.0168	1.43	
142	57991.4585129735	1758.1757	203.4843	5530	1400	0.029	0.0064	0.0218	0.0144	1.79	
143	57991.4608681160	1758.1780	245.9356	7530	1400	0.054	0.0063	0.0272	0.011	1.08	
144	57991.4637145928	1758.1809	19.4120	6750	1900	0.0731	0.0074	0.0471	0.013	1.08	
145	57991.4639392697	1758.1811	0.0024	5480	3000	0.0573	0.0092	0.0367	0.0161	1.08	
146	57991.4639392978	1758.1811	539.7461	5480	2000	0.0388	0.0075	0.0439	0.0152	1.43	
147	57991.4701863590	1758.1873	82.9205	6220	1400	0.0452	0.0064	0.0205	0.0091	0.72	
148	57991.4711460870	1758.1883	149.1976	6620	1500	0.0308	0.0065	0.0272	0.0161	2.15	
149	57991.4728729109	1758.1900	618.5275	5060	900	0.0255	0.0051	0.0201	0.0115	1.79	
150	57991.4800317945	1758.1972	740.5645	4830	2000	0.0469	0.0075	0.0353	0.0169	1.79	
151	57991.4886031426	1758.2058	393.6307	6420	900	0.0223	0.0051	0.0265	0.0145	2.87	
152	57991.4931590534	1758.2103	375.8981	5110	1900	0.0266	0.0073	0.0185	0.0166	1.79	
153	57991.4975097257	1758.2147	75.7672	4830	2000	0.0681	0.0075	0.05	0.0151	1.43	
154	57991.4983866613	1758.2155	37.0514	5940	900	0.0268	0.0051	0.0246	0.0127	2.15	
155	57991.4988154972	1758.2160	1040.3803	5530	2400	0.0417	0.0083	0.0515	0.0187	1.79	
156	57991.5108569357	1758.2280	194.5233	7330	2000	0.0555	0.0075	0.0241	0.0107	0.72	
157	57991.5131083628	1758.2303	528.9577	4830	2000	0.1284	0.0075	0.0964	0.0131	1.08	
158	57991.5192305588	1758.2364	0.0028	6910	2000	0.1106	0.0075	0.0498	0.0215	2.87	
159	57991.5192305898	1758.2364	3470.2810	6910	2000	0.0988	0.0075	0.0659	0.0152	1.43	
160	57991.5593958795	1758.2766	295.8331	6980	3900	0.0765	0.0105	0.0297	0.0151	0.72	
161	57991.5628198735	1758.2800	572.6219	6830	2800	0.1022	0.009	0.0585	0.0157	1.08	
162	57991.5694474415	1758.2866	134.2970	5950	2000	0.0448	0.0075	0.0696	0.0214	2.87	
163	57991.5710018046	1758.2882	297.4788	5670	1900	0.0434	0.0074	0.0492	0.0149	1.43	
164	57991.5744448464	1758.2916	1184.0859	6420	900	0.0183	0.0051	0.0177	0.0136	2.51	
165	57991.5881495443	1758.3053	204.0394	5580	2000	0.0679	0.0075	0.0478	0.0131	1.08	
166	57991.5905111113	1758.3077	138.2585	6410	2400	0.0644	0.0083	0.0421	0.0146	1.08	
167	57991.5921113250	1758.3093	286.5264	5940	2000	0.0862	0.0075	0.0518	0.0131	1.08	
168	57991.5954276026	1758.3126	28.6749	6250	1500	0.059	0.0065	0.0209	0.0093	0.72	
169	57991.5957594875	1758.3129	561.9668	6250	1500	0.0329	0.0065	0.0292	0.0131	1.43	
170	57991.6022637323	1758.3194		4920	1300	0.0601	0.0061	0.0213	0.0087	0.72	
171	57996.2656372	1762.9828		1400	300	24	7	35	10	2.6	0.40

Note: BPT: Barycentric peak time; TOA: time of arrival; WT: waiting time. S: peak flux; F: fluence. w: width, or the duration of the burst. For the references of the observational data, please see (Table 1).

Statistical Characteristics of Waiting Times

We use the available waiting time data for statistical analysis. The distribution of the waiting time is plotted as a histogram in (Figure 1). It can be clearly seen that there is a bimodal distribution. A small portion of the waiting times cluster in the range of 0.002-0.04 s. A Gaussian fit for them gives the peak time as $\Delta t \approx 0.0015$ s. It is very striking that FRBs could repeat after such a short quiescent period.

However, note that due to very limited number of events, significant fluctuation could be seen in the fit. In figure 1, most of the waiting times lie in the range of 1-6100 s. They can be well fitted by another Gaussian function with a reduced $\chi^2 \sim 6.259$ and aAdj. R-Square of ~ 0.945 . The peak value of the waiting time is $\Delta t = 169.93$ for these events. In our plot, since the X-axis is the logarithm of Δt , the Gaussian function means these waiting times follow a Log-normal distribution.

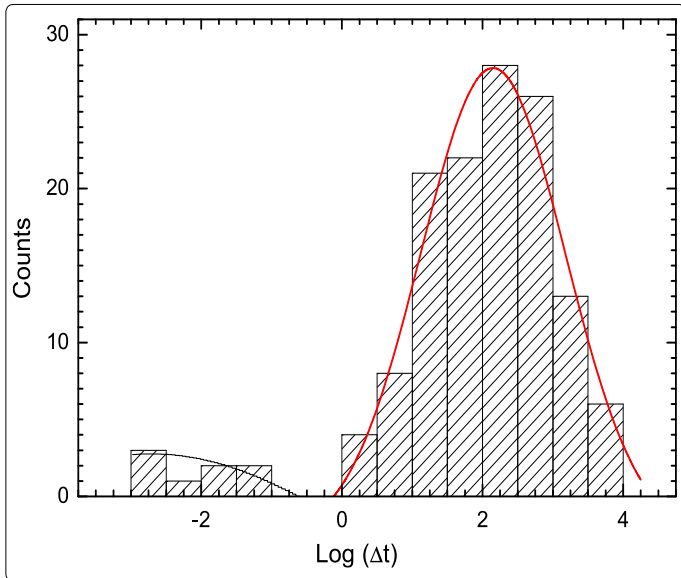


Figure 1. A histogram plot of the distribution of the waiting time (Δt , in units of s). The X-axis of the Δt data was logarithm, and the bin size is 0.5. A clear bimodal distribution can be seen. Most of the waiting times cluster at around several hundred seconds. They can be well fit by a Gaussian function, which means they follow a Log-normal distribution (the red line). A small portion of the waiting times are far below 1 millisecond. They still could be fit with a Gaussian function (the black line), but with significant fluctuation.

The cumulative distribution of the waiting time is shown in the (Figure 2). In this figure, the red line shows all the calculated waiting time data in (Table 2). However, since the bursts were observed at different frequencies by different receivers with different sensitivities, we have also plot the six sub-sets of data in the figure, i.e. GBT/C-band (4-8 GHz), GBT/S-band (1.6–2.4 GHz), AO/C-band (4.1–4.9GHz), AO/L-band and ALFA (1.2–1.5 GHz) and Eff/L-band (1.2-1.5 GHz), respectively. Generally speaking, these plots give us a straightforward vision of the effect of the telescope sensitivity. Due to the more efficient search technique of machine learning [99, 101], the contribution of the observation campaign at GBT/C-band is very striking.

According to some models, the energy released in an FRB burst are dependent on the quiescent period between two consecutive bursts, i.e., the waiting time. This is especially true for FRB models in which some kinds of intrinsic mechanisms are involved, such as the star quake models, the giant flare models of magnetars, the accretion-induced collapse of the crust of neutron stars or strange stars, etc. The reason is obvious: it is usually necessary for the system to accumulate some amount of energy to give birth to the next burst. As a result, the intensity of the burst should be correlated with the waiting time. On the contrary, in most models involving external mechanisms, no such correlation is expected. For example, if the FRB is produced by the collision of a small body or by many small bodies in an asteroid belt [62–64], the burst intensity will not correlate with the waiting time. So, the relationship between the burst intensity and the waiting time can provide valuable clues on the FRB models.

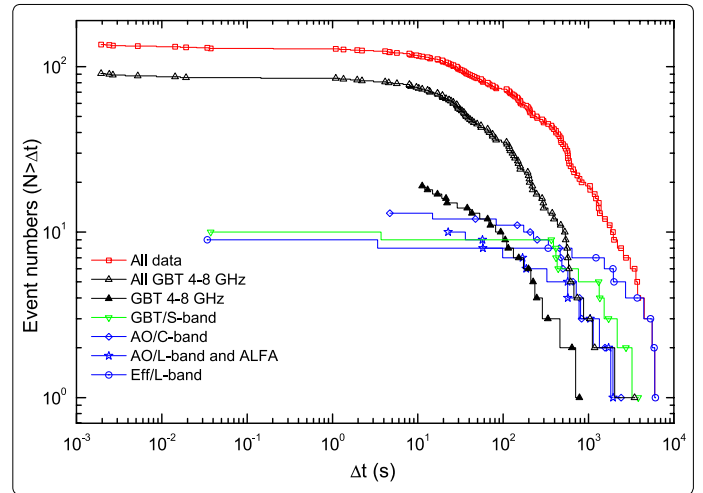


Figure 2. Cumulative distribution of the waiting time (Δt). The hollow red squares show all the waiting time available for FRB 121102, as listed in Table II. Other plots correspond to various sub-set of the data, i.e., the All GBT/4-8 GHz data (hollow black triangles) [101], part of the GBT/4-8 GHz data (filled black triangles) [99], the GBT/S-band data (opposite hollow triangles in green color) [93, 97], the AO/C-band data (hollow diamonds in blue) [77], the AO/L-band and ALFA data (hollow stars in blue) [92, 97], the Eff/L-band data (hollow circulars in blue) [94].

We have used our waiting time data to try to search for any possible correlation between the waiting time and the burst intensity. However, before presenting the results, it should be further noted that the waiting time actually could be correlated with either the preceding burst or the subsequent burst. We thus need to check these two cases separately.

In Figure 3, we plot the waiting time versus some interesting parameters, such as the peak flux density (S_{peak}), the duration (the Gaussian width, w), the fluence (F , which is calculated by multiplying S_{peak} and w). From figure 3, we can see the data points are widely scattered in all the plots, so that no obvious correlation can be observed between the burst intensity and the waiting time. This feature can provide us important clues about the nature of the repeating FRB source.

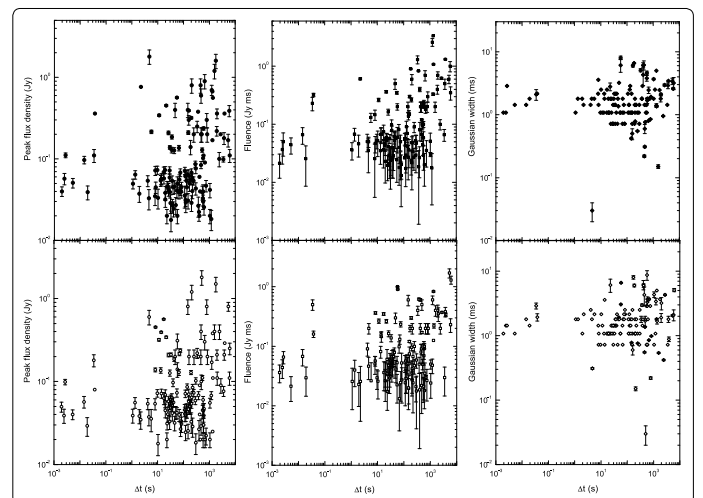


Figure 3. Waiting time (Δt) versus other three parameters of FRB bursts, i.e., the peak flux density (the left panels), the fluence (the middle panels), and the width (the right panels). In the upper three panels, the parameters are for the preceding bursts, while in the bottom three panels, the parameters are for the subsequent bursts. In all the plots, no obvious correlation can be seen between the three parameters and the waiting time.

As mentioned in Section I, all the FRB models proposed in the literature can be grouped into two different categories, i.e. catastrophic models and non-catastrophic models. For FRB 121102, surely only the non-catastrophic models can meet its basic requirement of repetition. It is interesting to note that the non-catastrophic models again can have two classes: those due to internal mechanisms and those due to external mechanisms. For example, most of the non-catastrophic models such as star quake-like explosions, flaring stars, lightning/wandering in pulsars, giant pulses/flares from young pulsars, collapse of strange star crusts, are all mechanisms involving internal processes. In these cases, the energy release is mainly caused by magnetic reconnection or accretion. So, to prepare for a new burst event, it usually takes a period of time to accumulate the energy. As a result, there is usually a positive correlation between the waiting time and the burst energetics. On the contrary, models involving the collisions between small bodies and neutron stars [62-64] are the few kinds of non-catastrophic models in which external mechanisms are engaged. In these cases, the happening of the bursts is almost completely random. The system does not need to accumulate any intension for the next burst. Therefore, the nonexistence of any correlation between the waiting time and other parameters (especially with the burst energetics) as shown in our figure 3 seem to rule out many intrinsic mechanism models for FRBs, but strongly support the external mechanism models, especially the collisions between small bodies and neutron stars [62-64].

Discussion and Conclusion

FRB 121102 is the only source that is observed to burst out repeatedly till now. In this study, we analyze the repeating behavior of FRB 121102 statistically, paying special attention on the waiting time. It is found that the waiting time shows a clear bimodal distribution, clustering at 0.002-0.04 s and 170 s respectively. It is striking to note that some bursts could happen very shortly after the preceding burst. We also tried to examine any possible correlation between the waiting time and the burst intensity. It is found that the waiting time does not correlate with the intensity (characterized by the peak flux and the burst fluence) of either the preceding burst or the subsequent burst. This result strongly indicates that the repeating bursts should be produced by some external mechanisms, but not intrinsic mechanisms. We suggest that the models involving collisions between small bodies and neutron stars [62-64] could be competitive mechanisms for FRBs.

Currently, due to the occultation of the Earth, FRB 121102 could not be continuously monitored for too long in any observational campaign. Usually, it could be continuously monitored for only one or two hours, and in a few very rare cases, the monitoring period could be extended to several hours. As a result, it is difficult for us to derive the waiting time that is longer than several thousands. This may be the reason that there is a cutoff at the longer section of the waiting time distribution. It is suggested the various large telescopes could cooperate to carry out an all-time monitoring campaign on

FRB 121102. It can help to clarify the waiting time distribution in the longer period regime, and may be important for understanding the nature of this enigmatic FRB source.

The bursts of FRB 121102 shows a clustering behavior in time. There are many outbursts in some particular time periods, which leads to very short waiting time for these bursts. For example, six bursts (Bursts 6 to 11) arrived in less than twenty minutes' period and four bursts (Bursts 13 to 16) occurred in a ~ 50 minutes' period during the Observation Campaign 4. Even more prominent is on the 33th and 34th observation campaign, where more frequent eruptions were observed within half an hour. It indicates that there appears to be epochs in which the source is more active. However, it should also be pointed out that there are also several very long observing sessions which resulted in non-detections [93, 95, 116]. The clustering phenomenon has been discussed by a few authors [117]. For example, a neutron star traveling through an asteroid belt can naturally lead to an active period and give birth to such a phenomenon [62-64]. In this case, the next active period could even be forecasted [119]. However, since FRB 121102 has been discovered for only less than 8 years, it is still an open question whether the repeating activity shows any difference on larger time-scales [120].

As shown in our figure 1, the majority of the waiting times follow a log-Gaussian distribution. This behavior is very similar to a few activities observed in other celestial objects, such as the waiting times of hard X-ray bursts from the Sun [118], the waiting times of hard X-ray bursts from the famous soft gamma-ray repeater SGR 1900+14 [105], and the waiting times of the Crab pulsar glitches ($\sim 10^2$ to $\sim 10^6$ s) [107]. In all these cases, the waiting times follow similar log-normal distributions. The common reason may be that they are all random processes to some extent.

In the bimodal distribution of the waiting time, there are about ten bursts clustered in the region with the waiting time less than 1 second, most of which were found by using the new searching technique [101]. However, while a few of these bursts are weak, there are also some strong bursts among them. It is thus even more difficult for the intrinsic mechanisms to explain such a fact: how the central engine could produce so many strong bursts in such a short period. On the contrary, this issue can be naturally accounted for by an external mechanism such as the collision between small bodies with neutron stars. It is possible that when a neutron star travels through an asteroid belt, it may encounter several asteroids one after the other, producing a group of bursts in a short time.

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